

**FORMAL LANGUAGES & AUTOMATA THEORY**

(Computer Science and Engineering)

Time: 3 hours

Max. Marks: 70

**PART – A**  
(Compulsory Question)

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- 1 Answer the following: (10 X 02 = 20 Marks)
- What is a string? How to concatenate two strings?
  - What is context free grammar?
  - Describe the language generated by the regular expression:  $(a + b)^*aaa(a + b)^*$ .
  - Let  $r_1$  be the regular expression representing the language  $L_1$ ,  $r_2$  be the regular expression representing the language  $L_2$ , what is the language represented by the regular expression  $r_2 + r_1$ .
  - Identify the language generated by context free grammar:  $S \rightarrow (S)|(O)|SS$ .
  - Define ambiguous grammar with example.
  - Can push down automata accept the regular language?
  - Give any two examples of languages that are accepted by PDA.
  - Define linear bounded automata.
  - Define multi-tape Turing machine.

**PART – B**

(Answer all five units, 5 X 10 = 50 Marks)

**UNIT – I**

- 2 (a) Construct the language generated by grammar  $S \rightarrow aSb/\epsilon$ .  
(b) Construct the language generated by the grammar  $S \rightarrow aCa; C \rightarrow aCa/b$ .

OR

- 3 Design a minimal DFA over the alphabet  $\Sigma = \{0, 1\}$  to accept the language  $L = \{w | w \cong 0 \pmod{3}\}$ .

**UNIT – II**

- 4 State and prove Arden's theorem.

OR

- 5 (a) Write the identities of regular expressions.  
(b) Draw the NFA to accept the languages generated by  $aa^*bb^*$

**UNIT – III**

- 6 (a) Remove unit productions in the following grammar:

$$\begin{aligned} S &\rightarrow ABaC \\ A &\rightarrow BC \\ B &\rightarrow b|\epsilon \\ C &\rightarrow D|\epsilon \\ D &\rightarrow \epsilon \end{aligned}$$

- (b) Remove unit productions in the following grammar:

$$\begin{aligned} S &\rightarrow aSb \\ S &\rightarrow A \\ A &\rightarrow cAd \\ A &\rightarrow cd \end{aligned}$$

OR

- 7 Define Chomsky normal form, convert the following grammar into CNF:

$$S \rightarrow bA|aB; A \rightarrow bAA|aS|a; B \rightarrow aBB|bS|a.$$

**UNIT – IV**

- 8 Construct a PDA that accepts the language generated by the following grammar:  $S \rightarrow aB; B \rightarrow bA/b; A \rightarrow aB$ .

OR

- 9 Construct a PDA to accept the language  $L = \{WCW^R | W \in (a, b)^+\}$  by the empty stack.

**UNIT – V**

- 10 Design a Turing machine to accept the language  $= \{a^n b^n, n \geq 1\}$ . Show an ID for the string 'aaabbb' with tape symbols.

OR

- 11 Write short notes on: (i) Instantaneous Description of TMs. (ii) Recursively Enumerable and Recursive Languages.

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