

DISCRETE MATHEMATICS
(Common to CSE and IT)

Time: 3 hours

Max. Marks: 70

PART – A
(Compulsory Question)

- 1 Answer the following: (10 X 02 = 20 Marks)
- Show the following implication without constructing the truth table: $(P \rightarrow Q) \rightarrow Q \Rightarrow P \vee Q$
 - State the pigeonhole principle.
 - State the properties of lattices.
 - Let (L, \leq) be a lattice and $a, b, c \in L$. Then prove $a \vee b = b$ iff $a \leq b$
 - In how many ways can 5 blue balls, 4 white balls and the rest 6 of different color balls be arranged in a row?
 - Define semi group.
 - What is the principle of mathematical induction?
 - Define the following terms. Give one suitable example for each:
 - Euler path.
 - Euler circuit.
 - Write about graph traversal techniques.
 - Write about isomorphic graphs.

PART – B
(Answer all five units, 5 X 10 = 50 Marks)

UNIT – I

- 2 (a) Show that among any 4 numbers one can find 2 numbers so that their difference is divisible by 3
(b) Show that among any $n+1$ numbers one can find 2 numbers so that their difference is divisible by n
- OR**
- 3 (a) Let $f: A \rightarrow \mathbb{R}$ be defined by $f(x) = (x-2) / (x-3)$, where $A = \mathbb{R} - \{3\}$. Is the function of objective? Find f^{-1} .
(b) Prove that $(A-B) \cup (B-A) = (A \cup B) - (A \cap B)$ for any two sets A and B .

UNIT – II

- 4 Let (L, \leq) be a lattice for any $a, b, c \in L$. Prove that $b \leq c \Rightarrow a * b \leq a * c \Rightarrow a \wedge b \leq a \wedge c$.
- OR**
- 5 (a) What is binary relation? Give properties of binary relation.
(b) Let $P(A)$ be the power set of any non empty set A , then prove that the relation \subset of set inclusion is not an equivalence relation.

UNIT – III

- 6 (a) Show that the set \mathbb{N} of natural numbers is a semi group under the operation $x * y = \max \{x, y\}$. Is it a monoid?
(b) Show that the set \mathbb{Z} with binary operation $*$ such that $x * y = x^y$ is not semi group.
- OR**
- 7 (a) In how many different ways can the letters of the word 'OPTICAL' be arranged so that the vowels always come together?
(b) In how many ways can a team of 5 persons can be formed out of a total of 10 persons such that two particular persons should not be included in any team?
(c) In a birthday party, every person shakes hand with every other person. If there was a total of 28 handshakes in the party, how many persons were present in the party?

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UNIT - IV

- 8 (a) Suppose that m is a fixed integer and $x \equiv y \pmod{m}$. Then for every integer $n \geq 1$, $x^n \equiv y^n \pmod{m}$. Prove this by mathematical induction
- (b) Suppose that $f(n) = n \cdot f(n-1)$ with $f(1) = 1$. Prove by induction that $f(n) = n \cdot (n-1) \cdot \dots \cdot 3 \cdot 2 \cdot 1$.

OR

- 9 (a) Solve the Recurrence relation $a_n = a_{n-1} + 6 a_{n-2}$ given the initial conditions $a_0 = 3$ and $a_1 = 6$.
- (b) Solve the recurrence relation $a_n = 7 a_{n-1} - 16 a_{n-2} + 12 a_{n-3} + n 4^n$, given $a_0 = -2$, $a_1 = 0$, $a_2 = 5$.

UNIT - V

- 10 (a) Explain Kruskal's algorithm with example.
- (b) When it can be said that two graphs G_1 and G_2 are isomorphic?

OR

- 11 (a) Explain DFS algorithm with an example.
- (b) Write about graph coloring.
