

**MATHEMATICS – III**

(Common to EEE, ECE and EIE)

Time: 3 hours

Max. Marks: 70

**PART – A**

(Compulsory Question)

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1 Answer the following: (10 X 02 = 20 Marks)

- (a) Evaluate  $\int_0^{\infty} e^{-\sqrt{x}} dx$ .
- (b) If  $P = 1/4$ , then  $\Gamma(P) \Gamma(1 - P) =$
- (c) In Rodrigue's formula,  $P_n(x) = CD^n\{(x^2 - 1)^n\}$  where  $C =$
- (d)  $\int J_0(x) J_1(x) dx =$
- (e) The harmonic conjugate of  $u(x, y) = x^2 - y^2$  is  $v =$
- (f) The mobius transformation that maps the points  $0, i, \infty$  respectively into  $0, 1, \infty$  is.....
- (g)  $\int_0^{1+i} z^2 dz =$ .
- (h) Define removable singularity with one example.
- (i) Taylor's series expansion for  $f(z) = (z - 1)/(z + 1)$  about  $z = 0$
- (j)  $\text{Res}_{z=-2}[z^2/(z - 1)(z + 2)^2] =$

**PART – B**

(Answer all five units, 5 X 10 = 50 Marks)

**UNIT - I**2 Express  $\int_0^3 \frac{dx}{\sqrt{9-x^2}}$  in terms of Beta function.

OR

3 Evaluate  $\int_0^2 (8 - x^3)^{-1/3} dx$  using  $\beta - \Gamma$  function.**UNIT - II**4 Show that  $J_n(x) = \frac{1}{\pi} \int_0^\pi (\cos n\theta - x \sin \theta) d\theta$ ,  $n$  being an integer.

OR

5 Prove that  $P_n(-x) = (-x)^n P_n(x)$ .**UNIT - III**6 Prove that  $u = e^{-x}[(x^2 - y^2)\cos y + 2xy\sin y]$  is harmonic and find the analytic function whose real part is  $u$ .

OR

7 Find the bilinear transformation that maps the points  $(0, 1, \infty)$  in the  $z$ -plane onto the points  $(-1, -2, -i)$  in the  $w$ -plane.**UNIT - IV**8 Evaluate  $\int_{(0,0)}^{(1,1)} [3x^2 + 5y + i(x^2 - y^2)] dz$  along  $y^2 = x$ .

OR

9 Find the Laurent series of  $\frac{z^2-1}{(z+2)(z+3)}$  for  $|z| > 3$ .**UNIT - V**10 Find the poles of  $f(z) = \frac{z^2-2z}{(z+1)^2(z^2+1)}$  and the residues at these poles.

OR

11 Show that  $\int_0^\infty \frac{x^2 dx}{(x^2+a^2)(x^2+b^2)} = \frac{\pi}{2(a+b)}$ .

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