

ADAPTIVE SIGNAL PROCESSING

(Common to SSP, DIP, CE&SP, IP, C&SP, SP&C)

Time: 3 Hours

Max Marks: 60

Answer any FIVE questions

All questions carry EQUAL marks

- 1 a Draw the block diagram of a generic adaptive filter and briefly state its aim. (6M)
 b Explain the nonlinear adaptive filtering with multiplier perceptrons (6M)

- 2 Given the tap delay line vector and coefficient vector of an adaptive filter of length L ,

$$\underline{x}_n = \begin{bmatrix} x[n] \\ x[n-1] \\ \vdots \\ x[n-L+1] \end{bmatrix} \quad \underline{w} = \begin{bmatrix} w_0^* \\ w_1^* \\ \vdots \\ w_{L-1}^* \end{bmatrix}$$

derive the Wiener-Hopf equation from the principle of orthogonality,
 $E\{\underline{x}_n e^*[n]\} = \underline{0}$, where $e[n]$ is the error signal.

(12M)

- 3 a Discuss the similarities and differences between the method of steepest descent and a stochastic gradient approach. (6M)

- b Explain Gradient Search by Newton's Method (6M)

- 4 a Derive a practical step size bound for the LMS algorithm from equation $\underline{v}_{n+1} = (\underline{I} - \mu \underline{\Lambda}) \underline{v}_n$ (6M)

whereby $\underline{v}_n = \underline{Q}(E\{\underline{w}_n\} - \underline{w}_{opt})$ with the eigenvalue decomposition

$$\underline{R} = \underline{Q} \cdot \underline{\Lambda} \cdot \underline{Q}^H$$

(6M)

- b Explain the Stability and Performance analysis of LMS Algorithms.

- 5 a Explain the procedural steps for Kalman Filter (6M)

- b Define Innovation Process and Kalman Gain (6M)

- 6 a Explain the Principle of Orthogonality? Give the mathematical representation (6M)

- b What are the two aspects of the performance of an adaptive filter? Explain (6M)

- 7 a Explain the RLS Algorithm (6M)

- b Explain the Adaptive Linear Combiner (6M)

- 8 Write short notes on the following (12M)